MATH 5: HOMEWORK 13

1. If $a = 2^{-13}3^9$, $b = 2^{11}3^{-7}$, what is the value of ab? of a/b?

2. In how many zeroes does the number $4^{15}5^{26}$ end?

3. Simplify:

(a)
$$(4c^2 \cdot c^3)^3$$
 (c) $((x^2y)^3)^4$ (e) $\left(\frac{9a^7b^6}{45a^3b}\right)^4$
(b) $\left(\frac{8dg^2}{3d^3g^4}\right)^3$ (d) $\frac{26(a^2b)^4}{65a^3b^2c^3}$ (f) $\left(\frac{3a^5b^2}{21ab}\right)^4 \cdot \frac{7^4}{a^{16}b^2}$

4. Let
$$x = a^3 \cdot b^2$$
, $y = \frac{b^5}{a^2 c^4}$, and $z = \frac{c^3}{ab}$. Express in terms of a, b, c :
(a) $(xy)^2 z$
(b) $\frac{x}{y}$
(c) $\frac{x^3 y^2}{xy^2 z^3}$

5. Suppose \$100 is deposited into an account and the amount doubles every 8 years. How much will be in the account after 40 years? Express your answer using powers.

6. At the beginning of an epidemic, 50 people are sick. If the number of sick people triples every other day, how many people will be sick at the end of 2 weeks? Express your answer using powers.

7. About how many hydrogen atoms are there in one gram of hydrogen?

- 8. Write the following numbers using scientific notation.
 - (a) the distance from Earth to Pluto is \approx 7,527,000,000 km;
 - (b) the distance from Earth to the star Sirius is \approx 81,900,000,000 km;
 - (c) the distance from Earth to Vega is \approx 249,500,000,000 km;
 - (d) the distance from Earth to the Andromeda Nebula is \approx 2,000,000,000,000,000,000 km.
 - (e) the area of the Pacific Ocean is $\approx 178{,}684{,}000{,}000~km^2$

9. Write the following numbers in regular form:

(a)
$$9.21 \times 10^6 =$$
 (b) $1.527 \times 10^4 =$
(c) $5.3459 \times 10^3 =$ (d) $7.527 \times 10^2 =$