MATH 5: WORKSHEET 11

1. Solve the following equations

(a)
$$5 - x = -4 - 2x$$

(b) $7 - 2(1 - x) = -5$
(c) $\frac{x - 2}{x - 1} = 3$

- **2.** Father is 32 years old and son is 5 years old. In how many years will the father be 10 times older than the son?
- **3.** Simplify the following expression:

$$\frac{(x^2y^2)\cdot x^3}{x^2y^5}$$

4. Let $a = 2 \cdot 10^8$, $b = 10^5$. Compute $a^2 \cdot b$, $\frac{a}{b}$, $a^2 \div b^3$.

- **5.** How many cubic centimeters are there in one cubic kilometer? (1 km =1000 m, 1 m=100 cm).
- 6. It is known that $2^{10} = 1024$, which is very close to 10^3 . Using this, can you estimate what is the value of 2^{20} ? 2^{32} ?
- *7. Consider the sequence 7, 7^2 , 7^3 , ... 7^n ...
 - (a) Show that there will be two numbers in this sequence which have the same last two digits. [Hint: pigeonhole principle!]
 - (b) Show that from some moment, the last two digits of numbers in this sequence will start repeating periodically.
- 8. (from 101 puzzles in thought and logic, by C. R. Wylie)

Clark, Jones, Morgan, and Smith are four men whose occupation are butcher, druggist, grocer, and policeman, though not necessarily in that order.

Clark and Jones are neighbors and take turns driving each other to work

Jones makes more money than Morgan

Clark beats Smith regularly at bowling

The butcher always walks to work

The policeman doesn't live near the druggist

The only time the grocer and the policeman ever meet is when the policeman arrested the grocer for speeding

The policeman makes more money than the druggist or the grocer

What is each man's occupation?