

**MATH 5: HANDOUT 12
POWERS.**

POWERS

Notation (n is a whole number):

$$a^n = \underbrace{a \cdot a \cdots a}_{n \text{ times}}$$

In particular,

$$a^1 = a$$

$$a^2 = a \cdot a \quad \text{reads "a square"}$$

$$a^3 = a \cdot a \cdot a \quad \text{reads "a cube"}$$

Properties:

$$(ab)^n = \underbrace{ab \cdot ab \cdots ab}_{n \text{ times}} = \underbrace{a \cdot a \cdots a}_{n \text{ times}} \cdot \underbrace{b \cdot b \cdots b}_{n \text{ times}} = a^n b^n$$

$$a^m a^n = \underbrace{a \cdot a \cdots a}_{m \text{ times}} \cdot \underbrace{a \cdot a \cdots a}_{n \text{ times}} = \underbrace{a \cdot a \cdots a}_{m+n \text{ times}} = a^{m+n}$$

$$(1) \quad \left(\frac{a}{b}\right)^n = \underbrace{\frac{a}{b} \cdot \frac{a}{b} \cdots \frac{a}{b}}_{n \text{ times}} = \frac{a^n}{b^n}$$

$$\frac{a^m}{a^n} = \frac{\overbrace{a \cdot a \cdots a}^{m \text{ times}}}{\underbrace{a \cdot a \cdots a}_{n \text{ times}}} = \underbrace{a \cdot a \cdots a}_{m-n \text{ times}} = a^{m-n} \quad \text{if } m > n$$

Homework problems on back

HOMWORK

For the homework, let me remind you that you should write solutions, showing your calculations and your reasoning — not just answers! Do not write on this homework assignment — use a separate sheet of paper instead; leave the homework assignment in your folder for future reference.

1. Solve the following equations

$$(a) 5 - x = -4 - 2x$$

$$(b) 7 - 2(1 - x) = -5$$

$$(c) \frac{x - 2}{x - 1} = 3$$

2. Father is 32 years old and son is 5 years old. In how many years will the father be 10 times older than the son?

3. Simplify

$$(a^2)(a^3)(a^4)$$

$$(p^3)(p^4)(p^6)(q^2)$$

$$(a^2b^3)(b^4a^3)$$

$$(x^4y^3)(y^6x^8)$$

$$\frac{a^3}{a^2}$$

$$\frac{x^5y^3}{x^2}$$

4. Let $a = 2 \cdot 10^8$, $b = 10^5$. Compute $a^2 \cdot b$, $\frac{a}{b}$, $a^2 \div b^3$.

5. How many cubic centimeters are there in one cubic kilometer? (1 km = 1000 m, 1 m = 100 cm).

6. (from *101 puzzles in thought and logic*, by C. R. Wylie)

Clark, Jones, Morgan, and Smith are four men whose occupation are butcher, druggist, grocer, and policeman, though not necessarily in that order.

Clark and Jones are neighbors and take turns driving each other to work

Jones makes more money than Morgan

Clark beats Smith regularly at bowling

The butcher always walks to work

The policeman doesn't live near the druggist

The only time the grocer and the policeman ever meet is when the policeman arrested the grocer for speeding

The policeman makes more money than the druggist or the grocer

What is each man's occupation?